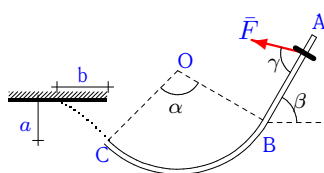


## Основные теоремы динамики точки

На прямолинейном участке пути шайба разгоняется в течение времени  $t = t_1$  переменной силой  $F$ , направленной под углом  $\gamma$  к перемещению. На криволинейном участке оси, изогнутой по дуге окружности радиуса  $r$  (геометрический центр в точке  $O$ ), действует постоянная сила сопротивления  $F_{fr}$ . Участки оси сопрягаются в точке  $B$  без излома. Вся траектория находится в вертикальной плоскости. Сила  $F$  дана в Н. В зависимости от варианта найти расстояние  $b$ , скорость  $v_A$  или силу  $F_{fr}$ .

### Задача 1.1

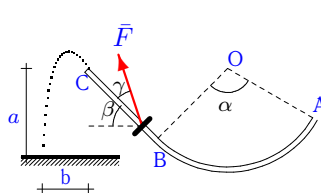
3



$$\begin{aligned} r &= 4 \text{ м}, m = 0.4 \text{ кг}, \\ a &= 14 \text{ м}, t_1 = 2 \text{ с}, \\ F &= 4 \sin \frac{\pi t}{2} + 5t, \\ v_A &= 25 \frac{\text{м}}{\text{с}}, F_{fr} - ? \\ b &= 80.7 \text{ м}. \\ \alpha &= 75^\circ, \beta = 60^\circ, \gamma = 45^\circ. \end{aligned}$$

### Задача 1.2

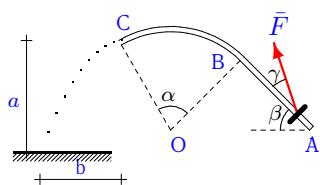
3



$$\begin{aligned} r &= 3 \text{ м}, m = 0.1 \text{ кг}, \\ a &= 2 \text{ м}, t_1 = 2 \text{ с}, \\ F &= 2 \cos^2 \frac{\pi t}{6}, \\ F_{fr} &= 5 \text{ Н}, v_A = 26 \frac{\text{м}}{\text{с}}, \\ b &- ? \\ \alpha &= 45^\circ, \beta = 30^\circ, \gamma = 15^\circ. \end{aligned}$$

### Задача 1.3

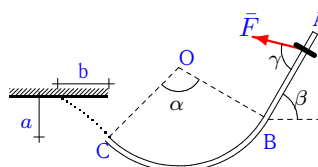
3



$$\begin{aligned} r &= 3 \text{ м}, m = 0.8 \text{ кг}, \\ a &= 10 \text{ м}, t_1 = 3 \text{ с}, \\ F &= 2 \sin \frac{\pi t}{3} + 9, \\ F_{fr} &= 11 \text{ Н}, b = 28.4 \text{ м}, \\ v_A &- ? \\ \alpha &= 60^\circ, \beta = 45^\circ, \gamma = 15^\circ. \end{aligned}$$

### Задача 1.4

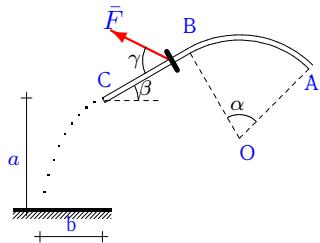
3



$$\begin{aligned} r &= 4 \text{ м}, m = 0.5 \text{ кг}, \\ a &= 5 \text{ м}, t_1 = 2 \text{ с}, \\ F &= 2 \cos \frac{\pi t}{5} + 4, \\ F_{fr} &= 5 \text{ Н}, b = 23.9 \text{ м}, \\ v_A &- ? \\ \alpha &= 30^\circ, \beta = 15^\circ, \gamma = 45^\circ. \end{aligned}$$

### Задача 1.5

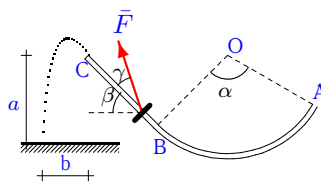
3



$$\begin{aligned} r &= 5 \text{ м}, m = 0.5 \text{ кг}, \\ a &= 7 \text{ м}, t_1 = 1 \text{ с}, \\ F &= 10 \sin^2(\pi t/6), \\ v_A &= 27 \frac{\text{м}}{\text{с}}, F_{fr} - ? \\ b &= 6.7 \text{ м}. \\ \alpha &= 60^\circ, \beta = 45^\circ, \gamma = 30^\circ. \end{aligned}$$

### Задача 1.6

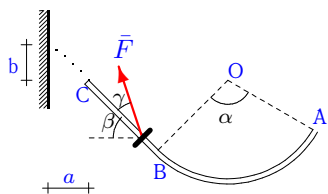
3



$$\begin{aligned} r &= 5 \text{ м}, m = 0.2 \text{ кг}, \\ a &= 3 \text{ м}, t_1 = 2 \text{ с}, \\ F &= \sqrt{2t+1}, \\ F_{fr} &= 1 \text{ Н}, b = 83 \text{ м}, \\ v_A &- ? \\ \alpha &= 60^\circ, \beta = 45^\circ, \gamma = 15^\circ. \end{aligned}$$

### Задача 1.7

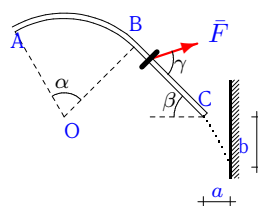
3



$$\begin{aligned} r &= 5 \text{ м}, m = 0.2 \text{ кг}, \\ a &= 110 \text{ м}, t_1 = 4 \text{ с}, \\ F &= 8t^2/(1+5t), \\ F_{fr} &= 4 \text{ Н}, b = 205.3 \text{ м}, \\ v_A &- ? \\ \alpha &= 90^\circ, \beta = 75^\circ, \gamma = 30^\circ. \end{aligned}$$

### Задача 1.8

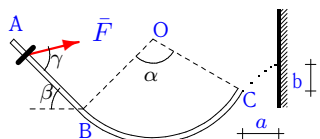
3



$$\begin{aligned} r &= 6 \text{ м}, m = 0.8 \text{ кг}, \\ a &= 60 \text{ м}, t_1 = 1 \text{ с}, \\ F &= 2 \sin \frac{\pi t}{3} + 9, \\ F_{fr} &= 11 \text{ Н}, b = 90 \text{ м}, \\ v_A &- ? \\ \alpha &= 60^\circ, \beta = 45^\circ, \gamma = 60^\circ. \end{aligned}$$

### Задача 1.9

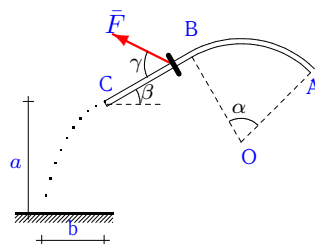
3



$$\begin{aligned} r &= 5 \text{ м}, m = 1 \text{ кг}, \\ a &= 11 \text{ м}, t_1 = 5 \text{ с}, \\ F &= 9t^2/(2+t^3), \\ F_{fr} &= 6 \text{ Н}, v_A = 26 \frac{\text{м}}{\text{с}}, \\ b &- ? \\ \alpha &= 75^\circ, \beta = 60^\circ, \gamma = 60^\circ. \end{aligned}$$

### Задача 1.10

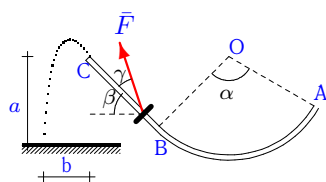
3



$$\begin{aligned} r &= 5 \text{ м}, m = 0.2 \text{ кг}, \\ a &= 1 \text{ м}, t_1 = 1 \text{ с}, \\ F &= 0.2 \exp(\frac{t}{5}) + 1, \\ F_{fr} &= 9 \text{ Н}, v_A = 25 \frac{\text{м}}{\text{с}}, \\ b &- ? \\ \alpha &= 45^\circ, \beta = 30^\circ, \gamma = 30^\circ. \end{aligned}$$

### Задача 1.11

3



$$r = 4 \text{ м}, m = 0.6 \text{ кг},$$

$$a = 4 \text{ м}, t_1 = 2 \text{ с},$$

$$F = 4 \cos \frac{\pi t}{3} + 3t,$$

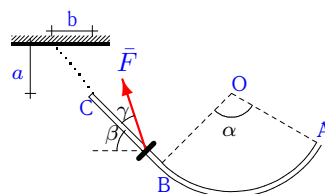
$$F_{fr} = 15 \text{ Н}, v_A = 26 \frac{\text{м}}{\text{с}},$$

$$b = ?$$

$$\alpha = 30^\circ, \beta = 15^\circ, \gamma = 15^\circ.$$

### Задача 1.12

3



$$r = 4 \text{ м}, m = 0.8 \text{ кг},$$

$$a = 10 \text{ м}, t_1 = 4 \text{ с},$$

$$F = 2 \sin \frac{\pi t}{3} + 9,$$

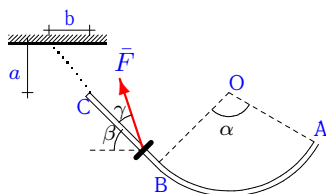
$$v_A = 26 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 10.6 \text{ м}.$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 15^\circ.$$

### Задача 1.13

3



$$r = 3 \text{ м}, m = 0.4 \text{ кг},$$

$$a = 6 \text{ м}, t_1 = 4 \text{ с},$$

$$F = 10/(1 + 2t),$$

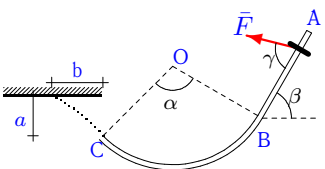
$$v_A = 25 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 4.2 \text{ м}.$$

$$\alpha = 75^\circ, \beta = 60^\circ, \gamma = 15^\circ.$$

### Задача 1.14

3



$$r = 5 \text{ м}, m = 0.5 \text{ кг},$$

$$a = 7 \text{ м}, t_1 = 2 \text{ с},$$

$$F = 10 \sin^2(\pi t/6),$$

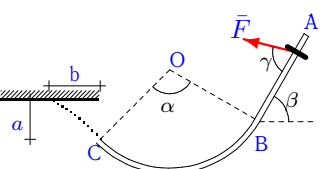
$$F_{fr} = 1 \text{ Н}, b = 37.5 \text{ м},$$

$$v_A = ?$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 45^\circ.$$

### Задача 1.15

3



$$r = 4 \text{ м}, m = 0.8 \text{ кг},$$

$$a = 10 \text{ м}, t_1 = 2 \text{ с},$$

$$F = 2 \sin \frac{\pi t}{3} + 9,$$

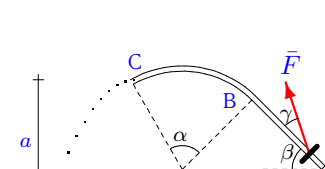
$$F_{fr} = 11 \text{ Н}, v_A = 26 \frac{\text{м}}{\text{с}},$$

$$b = ?$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 45^\circ.$$

### Задача 1.16

3



$$r = 4 \text{ м}, m = 0.5 \text{ кг},$$

$$a = 7 \text{ м}, t_1 = 3 \text{ с},$$

$$F = 10 \sin^2(\pi t/6),$$

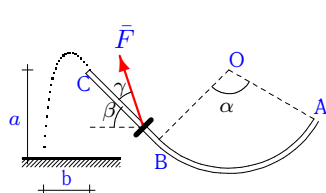
$$F_{fr} = 1 \text{ Н}, b = 19.7 \text{ м},$$

$$v_A = ?$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 15^\circ.$$

### Задача 1.17

3



$$r = 5 \text{ м}, m = 0.5 \text{ кг},$$

$$a = 7 \text{ м}, t_1 = 2 \text{ с},$$

$$F = 10 \sin^2(\pi t/6),$$

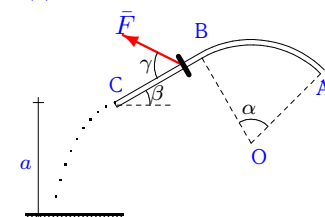
$$F_{fr} = 1 \text{ Н}, b = 58.1 \text{ м},$$

$$v_A = ?$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 15^\circ.$$

### Задача 1.18

3



$$r = 4 \text{ м}, m = 0.5 \text{ кг},$$

$$a = 9 \text{ м}, t_1 = 1 \text{ с},$$

$$F = 3 \cos \frac{\pi t}{2} + 4t,$$

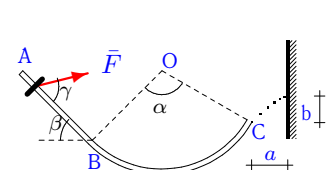
$$F_{fr} = 7 \text{ Н}, b = 2.3 \text{ м},$$

$$v_A = ?$$

$$\alpha = 90^\circ, \beta = 75^\circ, \gamma = 30^\circ.$$

### Задача 1.19

3



$$r = 4 \text{ м}, m = 1 \text{ кг},$$

$$a = 8 \text{ м}, t_1 = 5 \text{ с},$$

$$F = 8t^2/(1 + 5t),$$

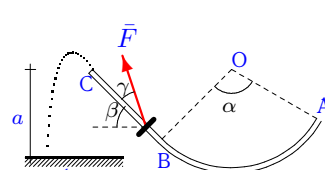
$$v_A = 26 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 2.07 \text{ м}.$$

$$\alpha = 90^\circ, \beta = 75^\circ, \gamma = 60^\circ.$$

### Задача 1.20

3



$$r = 5 \text{ м}, m = 0.4 \text{ кг},$$

$$a = 6 \text{ м}, t_1 = 2 \text{ с},$$

$$F = 10/(1 + 2t),$$

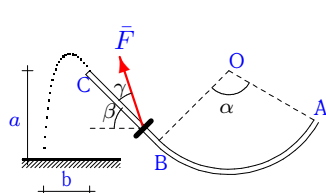
$$F_{fr} = 2 \text{ Н}, b = 63.9 \text{ м},$$

$$v_A = ?$$

$$\alpha = 75^\circ, \beta = 60^\circ, \gamma = 15^\circ.$$

### Задача 1.21

3



$$r = 6 \text{ м}, m = 0.5 \text{ кг},$$

$$a = 5 \text{ м}, t_1 = 2 \text{ с},$$

$$F = 2 \cos \frac{\pi t}{5} + 4,$$

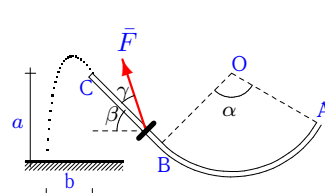
$$F_{fr} = 5 \text{ Н}, v_A = 27 \frac{\text{м}}{\text{с}},$$

$$b = ?$$

$$\alpha = 30^\circ, \beta = 15^\circ, \gamma = 15^\circ.$$

### Задача 1.22

3



$$r = 4 \text{ м}, m = 0.2 \text{ кг},$$

$$a = 3 \text{ м}, t_1 = 2 \text{ с},$$

$$F = \sqrt{2t + 1},$$

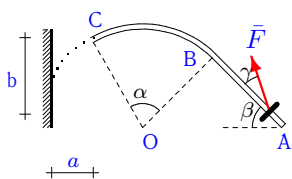
$$v_A = 25 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 73.1 \text{ м}.$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 15^\circ.$$

### Задача 1.23

3



$$r = 3 \text{ м}, m = 0.2 \text{ кг},$$

$$a = 3 \text{ м}, t_1 = 3 \text{ с},$$

$$F = \sqrt{2t + 1},$$

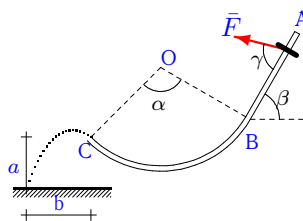
$$F_{fr} = 1 \text{ Н}, v_A = 26 \frac{\text{м}}{\text{с}},$$

$$b = ?$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 15^\circ.$$

### Задача 1.24

3



$$r = 4 \text{ м}, m = 0.2 \text{ кг},$$

$$a = 22 \text{ м}, t_1 = 5 \text{ с},$$

$$F = 7e^{2t}/(1 + e^{2t}),$$

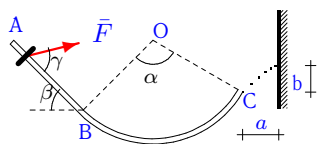
$$F_{fr} = 2 \text{ Н}, b = 597.5 \text{ м},$$

$$v_A = ?$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 75^\circ.$$

### Задача 1.25

3



$$r = 5 \text{ м}, m = 4.5 \text{ кг},$$

$$a = 5 \text{ м}, t_1 = 5 \text{ с},$$

$$F = t\sqrt{t^2 + 1},$$

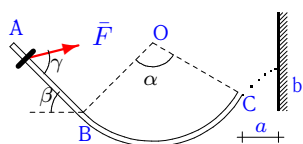
$$F_{fr} = 2 \text{ Н}, v_A = 26 \frac{\text{м}}{\text{с}},$$

$$b = ?$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 60^\circ.$$

### Задача 1.26

3



$$r = 4 \text{ м}, m = 2 \text{ кг},$$

$$a = 3 \text{ м}, t_1 = 5 \text{ с},$$

$$F = t \exp(t/4),$$

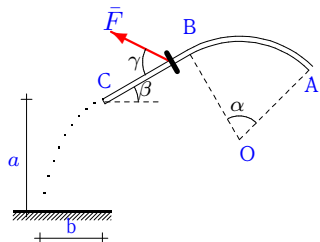
$$v_A = 27 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 0.77 \text{ м},$$

$$\alpha = 30^\circ, \beta = 15^\circ, \gamma = 60^\circ.$$

### Задача 1.27

3



$$r = 5 \text{ м}, m = 0.2 \text{ кг},$$

$$a = 3 \text{ м}, t_1 = 1 \text{ с},$$

$$F = \sqrt{2t + 1},$$

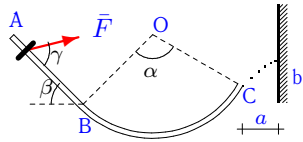
$$v_A = 26 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 2.9 \text{ м},$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 30^\circ.$$

### Задача 1.28

3



$$r = 4 \text{ м}, m = 0.5 \text{ кг},$$

$$a = 2 \text{ м}, t_1 = 5 \text{ с},$$

$$F = 2 \cos^2 \frac{\pi t}{6},$$

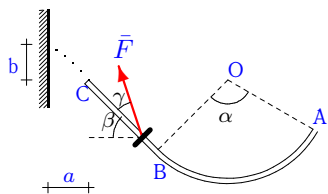
$$v_A = 25 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 0.52 \text{ м},$$

$$\alpha = 45^\circ, \beta = 30^\circ, \gamma = 60^\circ.$$

### Задача 1.29

3



$$r = 5 \text{ м}, m = 0.2 \text{ кг},$$

$$a = 1 \text{ м}, t_1 = 4 \text{ с},$$

$$F = 0.2 \exp(\frac{t}{5}) + 1,$$

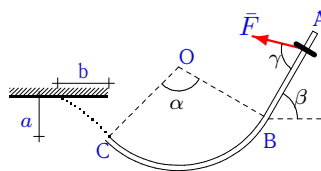
$$v_A = 27 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 0.56 \text{ м},$$

$$\alpha = 45^\circ, \beta = 30^\circ, \gamma = 30^\circ.$$

### Задача 1.30

3



$$r = 4 \text{ м}, m = 0.2 \text{ кг},$$

$$a = 1 \text{ м}, t_1 = 2 \text{ с},$$

$$F = 0.2 \exp(\frac{t}{5}) + 1,$$

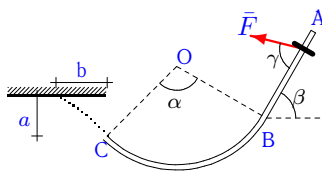
$$F_{fr} = 9 \text{ Н}, b = 3.9 \text{ м},$$

$$v_A = ?$$

$$\alpha = 45^\circ, \beta = 30^\circ, \gamma = 45^\circ.$$

### Задача 1.31

3



$$r = 4 \text{ м}, m = 0.6 \text{ кг},$$

$$a = 4 \text{ м}, t_1 = 2 \text{ с},$$

$$F = 4 \cos \frac{\pi t}{3} + 3t,$$

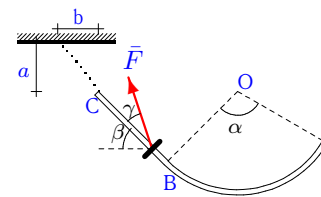
$$F_{fr} = 15 \text{ Н}, v_A = 26 \frac{\text{м}}{\text{с}},$$

$$b = ?$$

$$\alpha = 30^\circ, \beta = 15^\circ, \gamma = 45^\circ.$$

### Задача 1.32

3



$$r = 4 \text{ м}, m = 0.2 \text{ кг},$$

$$a = 3 \text{ м}, t_1 = 4 \text{ с},$$

$$F = \sqrt{2t + 1},$$

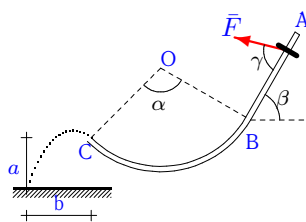
$$F_{fr} = 1 \text{ Н}, v_A = 25 \frac{\text{м}}{\text{с}},$$

$$b = ?$$

$$\alpha = 60^\circ, \beta = 45^\circ, \gamma = 15^\circ.$$

### Задача 1.33

3



$$r = 4 \text{ м}, m = 0.4 \text{ кг},$$

$$a = 6 \text{ м}, t_1 = 5 \text{ с},$$

$$F = 10/(1 + 2t),$$

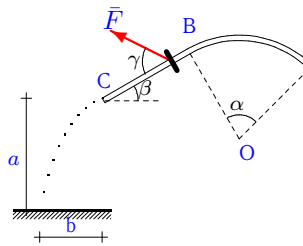
$$v_A = 26 \frac{\text{м}}{\text{с}}, F_{fr} = ?$$

$$b = 316.3 \text{ м},$$

$$\alpha = 75^\circ, \beta = 60^\circ, \gamma = 75^\circ.$$

### Задача 1.34

3



$$r = 6 \text{ м}, m = 0.9 \text{ кг},$$

$$a = 6 \text{ м}, t_1 = 1 \text{ с},$$

$$F = 3 \sin \frac{\pi t}{4} + t^2,$$

$$F_{fr} = 2 \text{ Н}, v_A = 27 \frac{\text{м}}{\text{с}},$$

$$b = ?$$

$$\alpha = 90^\circ, \beta = 75^\circ, \gamma = 30^\circ.$$

## Основные теоремы динамики точки

|    | $F_{tr}$ | $\int F dt$ | $v_A$  | $v_B$   | $v_C$   | $b$     |
|----|----------|-------------|--------|---------|---------|---------|
| 1  | 9.986    | 15.093      | 25.000 | 68.672  | 67.015  | 80.700  |
| 2  | 5.000    | 2.827       | 26.000 | 20.845  | 38.341  | 133.153 |
| 3  | 11.000   | 30.820      | 26.906 | 43.308  | 42.119  | 28.400  |
| 4  | 5.000    | 11.027      | 26.026 | 46.699  | 46.248  | 23.900  |
| 5  | -6.604   | 0.865       | 27.000 | 29.878  | 38.313  | 6.700   |
| 6  | 1.000    | 3.393       | 26.997 | 25.517  | 28.033  | 83.000  |
| 7  | 4.000    | 11.715      | 56.391 | 52.881  | 65.705  | 205.300 |
| 8  | 11.000   | 9.955       | 24.284 | 21.152  | 34.310  | 90.000  |
| 9  | 6.000    | 12.453      | 26.000 | 74.705  | 74.485  | 2.833   |
| 10 | 9.000    | 1.221       | 25.000 | 16.774  | 26.968  | 1.688   |
| 11 | 15.000   | 9.308       | 26.000 | 23.901  | 33.808  | 70.578  |
| 12 | 9.055    | 38.865      | 26.000 | 23.682  | 42.861  | 10.600  |
| 13 | 1.266    | 10.986      | 25.000 | 23.932  | 16.478  | 4.200   |
| 14 | 1.000    | 5.865       | 27.035 | 49.203  | 49.248  | 37.500  |
| 15 | 11.000   | 20.865      | 26.000 | 58.315  | 57.496  | 55.800  |
| 16 | 1.000    | 15.000      | 26.794 | 34.961  | 34.427  | 19.700  |
| 17 | 1.000    | 5.865       | 26.004 | 25.097  | 22.554  | 58.100  |
| 18 | 7.000    | 3.910       | 17.991 | 14.256  | 30.504  | 2.300   |
| 19 | 184.629  | 18.609      | 26.000 | 82.683  | 67.615  | 2.070   |
| 20 | 2.000    | 8.047       | 25.996 | 23.762  | 26.203  | 63.900  |
| 21 | 5.000    | 11.027      | 27.000 | 25.810  | 42.035  | 105.925 |
| 22 | 0.992    | 3.393       | 25.000 | 23.730  | 26.246  | 73.100  |
| 23 | 1.000    | 5.840       | 26.000 | 33.395  | 32.689  | 0.848   |
| 24 | 2.000    | 32.574      | 24.996 | 101.834 | 101.522 | 597.500 |
| 25 | 2.000    | 43.858      | 26.000 | 65.557  | 65.715  | 1.309   |
| 26 | 395.625  | 29.961      | 27.000 | 47.185  | 37.388  | 0.770   |
| 27 | 8.670    | 1.399       | 26.000 | 15.730  | 28.723  | 2.900   |
| 28 | 124.827  | 4.173       | 25.000 | 53.698  | 36.369  | 0.520   |
| 29 | 11.459   | 5.226       | 27.000 | 16.408  | 19.415  | 0.560   |
| 30 | 9.000    | 2.492       | 26.676 | 45.296  | 42.153  | 3.900   |
| 31 | 15.000   | 9.308       | 26.000 | 42.048  | 40.783  | 19.341  |
| 32 | 1.000    | 8.667       | 25.000 | 23.723  | 37.833  | 3.064   |
| 33 | 2.025    | 11.989      | 26.000 | 76.236  | 76.128  | 316.300 |
| 34 | 2.000    | 1.452       | 27.000 | 27.755  | 38.628  | 1.575   |