

Сферическое движение. Динамические уравнения Эйлера

Движение твердого тела, закрепленного шарнирно в начале координат, задано углами Эйлера. Найти модуль главного момента, приложенного к телу, при $t = 0$. Заданы главные моменты инерции тела (кгм²).

Литература. Тарг С.М. Краткий курс теоретической механики. - М.: Высш.шк., 1998, с. 150, 342.

Задача D37.1.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 3, \quad J_y = 5, \quad J_z = 4.$$

Задача D37.2.

2

$$\varphi = t + \pi/6, \quad \psi = 4t, \quad \theta = 2t + \pi/3, \\ J_x = 4, \quad J_y = 5, \quad J_z = 2.$$

Задача D37.3.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 5, \quad J_y = 3, \quad J_z = 4.$$

Задача D37.4.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 3, \quad J_y = 5, \quad J_z = 4.$$

Задача D37.5.

2

$$\varphi = 2t^2 + \pi/4, \quad \psi = 4t, \quad \theta = 3t + \pi/6, \\ J_x = 3, \quad J_y = 5, \quad J_z = 4.$$

Задача D37.6.

2

$$\varphi = 3t + \pi/3, \quad \psi = 4t^2, \quad \theta = 2t + \pi/2, \\ J_x = 1, \quad J_y = 5, \quad J_z = 5.$$

Задача D37.7.

2

$$\varphi = 2t^2 + \pi/4, \quad \psi = 4t, \quad \theta = 3t + \pi/6, \\ J_x = 3, \quad J_y = 5, \quad J_z = 4.$$

Задача D37.8.

2

$$\varphi = t^2 + \pi/4, \quad \psi = 4t, \quad \theta = 2t + \pi/6, \\ J_x = 4, \quad J_y = 2, \quad J_z = 5.$$

Задача D37.9.

2

$$\varphi = t + \pi/6, \quad \psi = 2t, \quad \theta = t + \pi/3, \\ J_x = 5, \quad J_y = 1, \quad J_z = 5.$$

Задача D37.10.

2

$$\varphi = t^2 + \pi/4, \quad \psi = 4t, \quad \theta = 2t + \pi/6, \\ J_x = 4, \quad J_y = 2, \quad J_z = 5.$$

Задача D37.11.

2

$$\varphi = 2t^2 + \pi/4, \quad \psi = 4t, \quad \theta = 3t + \pi/6, \\ J_x = 3, \quad J_y = 5, \quad J_z = 4.$$

Задача D37.12.

2

$$\varphi = 2t + \pi/3, \quad \psi = 2t^2, \quad \theta = 4t + \pi/2, \\ J_x = 4, \quad J_y = 5, \quad J_z = 2.$$

Задача D37.13.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 1, \quad J_y = 3, \quad J_z = 3.$$

Задача D37.14.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 3, \quad J_y = 2, \quad J_z = 2.$$

Задача D37.15.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 1, \quad J_y = 3, \quad J_z = 3.$$

Задача D37.16.

2

$$\varphi = 2t + \pi/3, \quad \psi = 2t^2, \quad \theta = 4t + \pi/2, \\ J_x = 5, \quad J_y = 3, \quad J_z = 4.$$

Задача D37.17.

2

$$\varphi = 2t^2 + \pi/4, \quad \psi = 4t, \quad \theta = t + \pi/6, \\ J_x = 6, \quad J_y = 4, \quad J_z = 4.$$

Задача D37.18.

2

$$\varphi = 2t + \pi/6, \quad \psi = 4t, \quad \theta = 2t + \pi/3, \\ J_x = 3, \quad J_y = 4, \quad J_z = 3.$$

Задача D37.19.

2

$$\varphi = 3t^2 + \pi/4, \quad \psi = 4t, \quad \theta = 3t + \pi/6, \\ J_x = 4, \quad J_y = 2, \quad J_z = 4.$$

Задача D37.20.

2

$$\varphi = 2t + \pi/6, \quad \psi = 4t, \quad \theta = 2t + \pi/3, \\ J_x = 5, \quad J_y = 4, \quad J_z = 3.$$

Задача D37.21.

2

$$\varphi = 3t + \pi/3, \quad \psi = 4t^2, \quad \theta = 2t + \pi/2, \\ J_x = 1, \quad J_y = 5, \quad J_z = 5.$$

Задача D37.22.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 2, \quad J_y = 4, \quad J_z = 3.$$

Задача D37.23.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 5, \quad J_y = 3, \quad J_z = 3.$$

Задача D37.24.

2

$$\varphi = 4t^2 + \pi/4, \quad \psi = 4t, \quad \theta = 2t + \pi/6, \\ J_x = 5, \quad J_y = 1, \quad J_z = 5.$$

Задача D37.25.

2

$$\varphi = 2t + \pi/6, \quad \psi = 4t, \quad \theta = 2t + \pi/3, \\ J_x = 5, \quad J_y = 4, \quad J_z = 5.$$

Задача D37.26.

2

$$\varphi = 3t^2 + \pi/4, \quad \psi = 4t, \quad \theta = 3t + \pi/6, \\ J_x = 4, \quad J_y = 2, \quad J_z = 4.$$

Задача D37.27.

2

$$\varphi = 2t + \pi/3, \quad \psi = 3t^2, \quad \theta = 2t + \pi/2, \\ J_x = 4, \quad J_y = 2, \quad J_z = 4.$$

Задача D37.28.

2

$$\varphi = 2t + \pi/3, \quad \psi = 4t^2, \quad \theta = 4t + \pi/2, \\ J_x = 4, \quad J_y = 2, \quad J_z = 3.$$

Задача D37.29.

2

$$\varphi = t + \pi/6, \quad \psi = 4t, \quad \theta = 2t + \pi/3, \\ J_x = 2, \quad J_y = 6, \quad J_z = 5.$$

Задача D37.30.

2

$$\varphi = 2t + \pi/3, \quad \psi = 2t^2, \quad \theta = 4t + \pi/2, \\ J_x = 3, \quad J_y = 1, \quad J_z = 3.$$

Задача D37.31.

2

$$\varphi = 3t^2 + \pi/4, \quad \psi = 2t, \quad \theta = t + \pi/6, \\ J_x = 5, \quad J_y = 3, \quad J_z = 5.$$

Задача D37.32.

2

$$\varphi = 2t + \pi/6, \quad \psi = 4t, \quad \theta = 2t + \pi/3, \\ J_x = 5, \quad J_y = 6, \quad J_z = 4.$$

Задача D37.33.

2

$$\varphi = 2t + \pi/3, \quad \psi = 3t^2, \quad \theta = 2t + \pi/2,$$

$$J_x = 4, \quad J_y = 2, \quad J_z = 4.$$

Задача D37.34.

2

$$\varphi = 2t + \pi/3, \quad \psi = 3t^2, \quad \theta = 2t + \pi/2,$$

$$J_x = 2, \quad J_y = 1, \quad J_z = 2.$$

D37 Ответы.**Сферическое движение. Динамические уравнения Эйлера**

17.09.2012

№	ω_x	ω_y	ω_z	M_x	M_y	M_z	M_0
1	2.000	-3.464	2.000	6.928	-4.000	-13.856	16.000
2	3.464	2.000	3.000	-2.000	20.785	-6.928	22.000
3	2.000	-3.464	2.000	-6.928	4.000	13.856	16.000
4	2.000	-3.464	2.000	6.928	-4.000	-13.856	16.000
5	3.536	-0.707	3.464	24.495	24.495	-13.000	37.000
6	1.000	-1.732	3.000	1.732	-7.000	-6.928	10.000
7	3.536	-0.707	3.464	24.495	24.495	-13.000	37.000
8	2.828	0.000	3.464	19.596	0.000	-10.000	22.000
9	1.732	1.000	2.000	15.500	-0.866	-15.588	22.000
10	2.828	0.000	3.464	19.596	0.000	-10.000	22.000
11	3.536	-0.707	3.464	24.495	24.495	-13.000	37.000
12	2.000	-3.464	2.000	6.928	-2.000	-6.928	10.000
13	2.000	-3.464	2.000	0.000	-8.000	-13.856	16.000
14	2.000	-3.464	2.000	0.000	4.000	6.928	8.000
15	2.000	-3.464	2.000	0.000	-8.000	-13.856	16.000
16	2.000	-3.464	2.000	-24.249	-2.000	13.856	28.000
17	2.121	0.707	3.464	14.697	24.495	5.000	29.000
18	3.464	2.000	4.000	10.000	-13.856	-13.856	22.000
19	3.536	-0.707	3.464	24.495	14.697	5.000	29.000
20	3.464	2.000	4.000	22.000	13.856	-27.713	38.000
21	1.000	-1.732	3.000	1.732	-7.000	-6.928	10.000
22	2.000	-3.464	2.000	6.928	-4.000	-13.856	16.000
23	2.000	-3.464	2.000	0.000	8.000	13.856	16.000
24	2.828	0.000	3.464	24.495	4.899	20.000	32.000
25	3.464	2.000	4.000	38.000	-13.856	-41.569	58.000
26	3.536	-0.707	3.464	24.495	14.697	5.000	29.000
27	1.000	-1.732	2.000	-0.000	2.000	3.464	4.000
28	2.000	-3.464	2.000	-6.928	4.000	13.856	16.000
29	3.464	2.000	3.000	2.000	-31.177	-6.928	32.000
30	2.000	-3.464	2.000	-24.249	-2.000	13.856	28.000
31	1.414	0.000	1.732	6.124	3.674	25.000	26.000
32	3.464	2.000	4.000	14.000	-6.928	-20.785	26.000
33	1.000	-1.732	2.000	-0.000	2.000	3.464	4.000
34	1.000	-1.732	2.000	-0.000	1.000	1.732	2.000