

Декартовы координаты. Пространственная траектория

Точка движется по закону $x = x(t), y = y(t), z = z(t)$. Определить скорость, ускорение точки и радиус кривизны траектории при $t = t_1$ (x, y и z даны в сантиметрах, t и t_1 — в секундах).

Кирсанов М.Н. **Решебник. Теоретическая механика**/Под ред. А. И. Кириллова.— М.: ФИЗМАТЛИТ, 2008. — 384 с. (с.137.)

Задача К2.1.

8

$$\begin{aligned}x &= 4\operatorname{tg}(t/3), \\y &= 8\sqrt{3t+8}, \\z &= 3\arcsin(t/8), \quad t_1 = 0.7.\end{aligned}$$

Задача К2.2.

8

$$\begin{aligned}x &= 18e^{t/4}, \\y &= \frac{1}{2}\sin^2 8t - 8t, \\z &= 7\ln(2t+2), \quad t_1 = 0.7.\end{aligned}$$

Задача К2.3.

8

$$\begin{aligned}x &= 9t + \frac{1}{2}\cos^2 6t, \\y &= 8\sqrt{3t+8}, \\z &= 2t^2 + 8t + 3, \quad t_1 = 0.7.\end{aligned}$$

Задача К2.4.

8

$$\begin{aligned}x &= 5t + \frac{1}{4}\cos^2 8t, \\y &= 2\arcsin(t/4), \\z &= 3\ln(4t+2), \quad t_1 = 0.3.\end{aligned}$$

Задача К2.5.

8

$$\begin{aligned}x &= 13e^{t/4}, \\y &= 4t + \cos^2 4t, \\z &= 3t^2 + 3t + 2, \quad t_1 = 0.2.\end{aligned}$$

Задача К2.6.

8

$$\begin{aligned}x &= \frac{7}{2t+3}, \\y &= 3\arcsin(t/4), \\z &= 4e^{(t^2)}, \quad t_1 = 0.3.\end{aligned}$$

Задача К2.7.

8

$$\begin{aligned}x &= 13e^{t/4}, \\y &= 2\ln(2t+2), \\z &= 5\operatorname{tg}(t/4), \quad t_1 = 0.2.\end{aligned}$$

Задача К2.8.

8

$$\begin{aligned}x &= 3t^2 + 10t + 2, \\y &= 20e^{t/4}, \\z &= 11t + \cos^2 4t, \quad t_1 = 0.9.\end{aligned}$$

Задача К2.9.

8

$$\begin{aligned}x &= \frac{1}{2}\sin 6t + 6t, \\y &= 6e^{(t^2)}, \\z &= 7(t+1)^{1/5}, \quad t_1 = 0.5.\end{aligned}$$

Задача К2.10.

8

$$\begin{aligned}x &= 3\ln(3t+2), \\y &= 2t^2 + 4t + 3, \\z &= 5t + \frac{1}{2}\cos^2 6t, \quad t_1 = 0.3.\end{aligned}$$

Задача K2.11.

8

$$\begin{aligned}x &= 6t + \frac{1}{4} \cos^2 8t, \\y &= 5e^{(t^2)}, \\z &= 5\sqrt{4t+5}, \quad t_1 = 0.4.\end{aligned}$$

Задача K2.13.

8

$$\begin{aligned}x &= 11(t+1)^{1/5}, \\y &= 20e^{t/3}, \\z &= 11(t+1)^{1/5}, \quad t_1 = 0.9.\end{aligned}$$

Задача K2.15.

8

$$\begin{aligned}x &= 18e^{t/3}, \\y &= 2t^2 + 8t + 3, \\z &= \frac{1}{2} \sin 6t + 8t, \quad t_1 = 0.7.\end{aligned}$$

Задача K2.17.

8

$$\begin{aligned}x &= 6(t+1)^{3/10}, \\y &= 5\operatorname{tg}(t/4), \\z &= 4\arcsin(t/5), \quad t_1 = 0.4.\end{aligned}$$

Задача K2.19.

8

$$\begin{aligned}x &= 6t + \frac{1}{2} \cos^2 6t, \\y &= 5\sqrt{3t+5}, \\z &= \frac{1}{2} \sin 6t + 5t, \quad t_1 = 0.4.\end{aligned}$$

Задача K2.21.

8

$$\begin{aligned}x &= 9\sqrt{3t+9}, \\y &= 9e^{(t^2)}, \\z &= 10t + \frac{1}{2} \cos^2 6t, \quad t_1 = 0.8.\end{aligned}$$

Задача K2.12.

8

$$\begin{aligned}x &= 4e^{(t^2)}, \\y &= 3 \ln(4t+2), \\z &= \frac{1}{2} \sin^2 4t - 4t, \quad t_1 = 0.3.\end{aligned}$$

Задача K2.14.

8

$$\begin{aligned}x &= \frac{1}{2} \sin 4t + 4t, \\y &= t^2 + 4t + 4, \\z &= 3\operatorname{tg}(t/2), \quad t_1 = 0.3.\end{aligned}$$

Задача K2.16.

8

$$\begin{aligned}x &= 4\sqrt{4t+4}, \\y &= 3\operatorname{tg}(t/2), \\z &= 5(t+1)^{1/10}, \quad t_1 = 0.3.\end{aligned}$$

Задача K2.18.

8

$$\begin{aligned}x &= \frac{1}{2} \sin^2 6t - 4t, \\y &= 2t^2 + 4t + 3, \\z &= 3\arcsin(t/4), \quad t_1 = 0.3.\end{aligned}$$

Задача K2.20.

8

$$\begin{aligned}x &= \frac{1}{2} \sin^2 8t - 7t, \\y &= \frac{10}{3t+4}, \\z &= \frac{1}{2} \sin 8t + 7t, \quad t_1 = 0.6.\end{aligned}$$

Задача K2.22.

8

$$\begin{aligned}x &= 3t + \cos^2 4t, \\y &= \frac{1}{2} \sin 8t + 2t, \\z &= 2\sqrt{2t+2}, \quad t_1 = 0.1.\end{aligned}$$

Задача K2.23.

8

$$\begin{aligned}x &= 2\arcsin(t/4), \\y &= 4\sqrt{4t+4}, \\z &= 14e^{t/2}, \quad t_1 = 0.3.\end{aligned}$$

Задача K2.24.

8

$$\begin{aligned}x &= 6\ln(3t+2), \\y &= \frac{10}{2t+3}, \\z &= 8t + \frac{1}{2}\cos^2 6t, \quad t_1 = 0.6.\end{aligned}$$

Задача K2.25.

8

$$\begin{aligned}x &= \frac{1}{2}\sin^2 4t - 11t, \\y &= 11\sqrt{4t+11}, \\z &= 11e^{(t^2)}, \quad t_1 = 1.\end{aligned}$$

Задача K2.26.

8

$$\begin{aligned}x &= \frac{1}{2}\sin^2 8t - 6t, \\y &= 5\ln(2t+2), \\z &= 7(t+1)^{3/10}, \quad t_1 = 0.5.\end{aligned}$$

Задача K2.27.

8

$$\begin{aligned}x &= 6\ln(3t+2), \\y &= 8t + \frac{1}{2}\cos^2 6t, \\z &= \frac{1}{2}\sin 6t + 7t, \quad t_1 = 0.6.\end{aligned}$$

Задача K2.28.

8

$$\begin{aligned}x &= 11(t+1)^{1/10}, \\y &= 9\ln(4t+2), \\z &= 10\sqrt{4t+10}, \quad t_1 = 0.9.\end{aligned}$$

Задача K2.29.

8

$$\begin{aligned}x &= 4\arcsin(t/8), \\y &= 18e^{t/4}, \\z &= 8e^{(t^2)}, \quad t_1 = 0.7.\end{aligned}$$

Задача K2.30.

8

$$\begin{aligned}x &= \frac{1}{2}\sin 8t + 4t, \\y &= 5\operatorname{tg}(t/4), \\z &= 4\arcsin(t/4), \quad t_1 = 0.3.\end{aligned}$$

Задача K2.31.

8

$$\begin{aligned}x &= 7e^{(t^2)}, \\y &= \frac{1}{2}\sin 8t + 7t, \\z &= 4\arcsin(t/7), \quad t_1 = 0.6.\end{aligned}$$

Задача K2.32.

8

$$\begin{aligned}x &= 11e^{(t^2)}, \\y &= \frac{1}{2}\sin^2 6t - 11t, \\z &= \frac{1}{2}\sin 6t + 11t, \quad t_1 = 1.\end{aligned}$$

Задача K2.33.

8

$$\begin{aligned}x &= 5\sqrt{2t+5}, \\y &= 6(t+1)^{3/10}, \\z &= \frac{8}{3t+4}, \quad t_1 = 0.4.\end{aligned}$$

Задача K2.34.

8

$$\begin{aligned}x &= \frac{9}{3t+4}, \\y &= 6e^{(t^2)}, \\z &= 6\sqrt{2t+6}, \quad t_1 = 0.5.\end{aligned}$$

К2 Ответы.**Декартовы координаты. Пространственная траектория** 07.04.2012

№	v_x	v_y	v_z	v	a_x	a_y	a_z	a	a_τ	a_n	R
1	1.41	3.78	0.38	4.05	0.22	-0.56	0.00	0.60	-0.45	0.41	40.186
2	5.36	-11.92	4.12	13.70	1.34	12.99	-2.42	13.28	-11.50	6.64	28.261
3	6.44	3.78	10.80	13.13	18.69	-0.56	4.00	19.13	12.30	14.65	11.763
4	6.99	0.50	3.75	7.95	-2.80	0.01	-4.69	5.46	-4.67	2.82	22.381
5	3.42	0.00	4.20	5.41	0.85	0.93	6.00	6.13	5.19	3.26	8.992
6	-1.08	0.75	2.63	2.94	1.20	0.01	10.33	10.40	8.80	5.55	1.556
7	3.42	1.67	1.25	4.00	0.85	-1.39	0.03	1.63	0.16	1.62	9.872
8	15.40	6.26	7.83	18.37	6.00	1.57	-19.47	20.43	-2.73	20.25	16.673
9	3.03	7.70	1.01	8.34	-2.54	23.11	-0.54	23.26	20.36	11.24	6.188
10	3.10	5.20	6.33	8.76	-3.21	4.00	32.28	32.69	24.56	21.57	3.556
11	5.77	4.69	3.89	8.39	-31.78	15.49	-1.18	35.38	-13.72	32.61	2.160
12	2.63	3.75	-2.65	5.29	10.33	-4.69	-11.80	16.37	7.71	14.43	1.938
13	1.32	9.00	1.32	9.19	-0.55	3.00	-0.55	3.10	2.78	1.38	61.400
14	4.72	4.60	1.53	6.77	-7.46	2.00	0.23	7.72	-3.79	6.73	6.812
15	7.58	10.80	6.53	14.72	2.53	4.00	15.69	16.39	11.19	11.97	18.106
16	3.51	1.53	0.39	3.85	-1.35	0.23	-0.27	1.40	-1.17	0.77	19.273
17	1.42	1.26	0.80	2.06	-0.71	0.06	0.01	0.71	-0.45	0.56	7.643
18	-5.33	5.20	0.75	7.48	-32.28	4.00	0.01	32.53	25.77	19.86	2.820
19	8.99	3.01	2.79	9.88	-3.15	-0.73	-12.16	12.58	-6.52	10.76	9.073
20	-7.70	-0.89	7.35	10.68	-63.02	0.92	31.88	70.63	67.28	21.49	5.307
21	4.00	27.31	10.52	29.54	-0.53	77.83	35.45	85.53	84.52	13.11	66.567
22	0.13	4.79	1.35	4.97	-22.29	-22.96	-0.61	32.01	-22.84	22.42	1.104
23	0.50	3.51	8.13	8.87	0.01	-1.35	4.07	4.28	3.19	2.85	27.569
24	4.74	-1.13	5.62	7.44	-3.74	1.08	-21.90	22.24	-19.10	11.41	4.847
25	-9.02	5.68	59.80	60.74	-2.33	-0.76	179.41	179.42	176.90	30.00	122.988
26	-2.04	3.33	1.58	4.22	-9.31	-2.22	-0.74	9.60	2.48	9.28	1.917
27	4.74	5.62	4.31	8.52	-3.74	-21.90	7.97	23.60	-12.49	20.02	3.625
28	0.62	6.43	5.42	8.43	-0.29	-4.59	-0.80	4.67	-4.03	2.35	30.247
29	0.50	5.36	18.28	19.06	0.01	1.34	51.71	51.73	49.98	13.33	27.250
30	1.05	1.26	1.00	1.92	-21.61	0.05	0.02	21.61	-11.78	18.12	0.204
31	12.04	7.35	0.57	14.12	34.51	31.88	0.01	46.98	46.03	9.41	21.179
32	59.80	-12.61	13.88	62.67	179.41	30.38	5.03	182.03	166.19	74.27	52.887
33	2.08	1.42	-0.89	2.67	-0.36	-0.71	1.02	1.30	-1.00	0.83	8.595
34	-0.89	7.70	2.27	8.08	0.97	23.11	-0.32	23.14	21.84	7.64	8.547

К2 файл о2к8А