

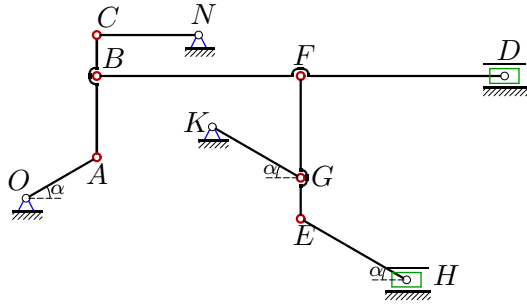
## Кинематический анализ механизма (7 звеньев)

Плоский многосвязный механизм с одной степенью свободы приводится в движение кривошипом, который вращается против часовой стрелки с постоянной угловой скоростью. Найти скорости всех шарниров механизма (в см/с) и ускорения трех заданных шарниров (в м/с<sup>2</sup>). Размеры даны в сантиметрах.

Кирсанов М.Н. **Решебник. Теоретическая механика**/Под ред. А. И. Кириллова. – М.: ФИЗМАТЛИТ, 2008. – 384 с. (с.158.)

### Задача К9.1.

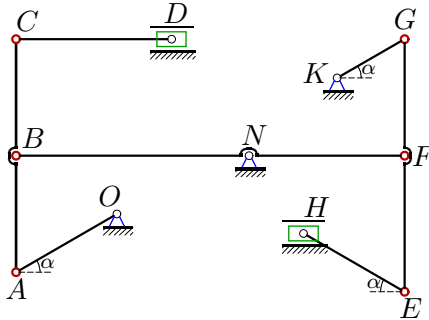
6



$\omega_{OA} = 3 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 20, BC = 10,$   
 $BF = 50, FD = 50,$   
 $NC = 25, EH = 30,$   
 $FE = 35, FG = 25,$   
 $OA = 20, KG = 25.$   
 $a_A, a_B, a_C - ?$

### Задача К9.2.

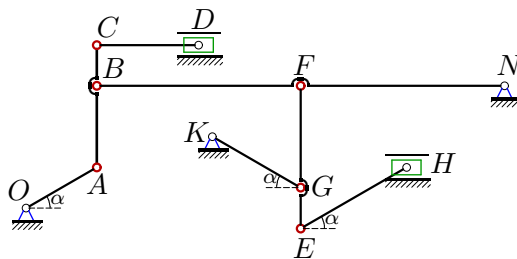
6



$\omega_{OA} = 3 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $NB = 60, NF = 40,$   
 $CD = 40, EH = 30,$   
 $FE = 35, FG = 30,$   
 $OA = 30, KG = 20.$   
 $a_A, a_B, a_C - ?$

### Задача К9.3.

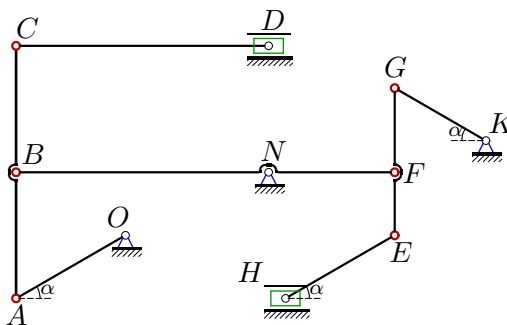
6



$\omega_{OA} = 4 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 20, BC = 10,$   
 $BF = 50, NF = 50,$   
 $CD = 25, EH = 30,$   
 $FG = 25, GE = 10,$   
 $OA = 20, KG = 25.$   
 $a_A, a_B, a_C - ?$

### Задача К9.4.

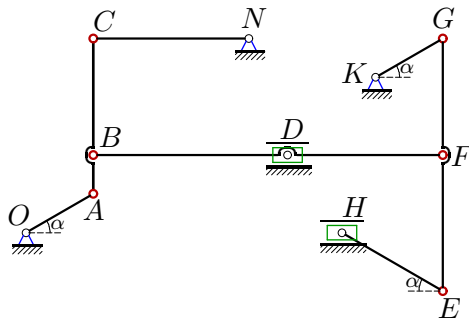
6



$\omega_{OA} = 1 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $NB = 60, NF = 30,$   
 $CD = 60, EH = 30,$   
 $FE = 15, FG = 20,$   
 $OA = 30, KG = 25.$   
 $a_A, a_B, a_C - ?$

**Задача K9.5.**

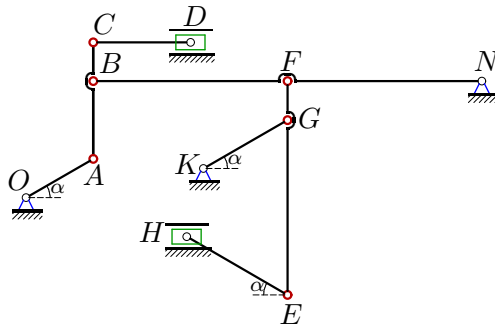
6



$\omega_{NC} = 4 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 10, BC = 30,$   
 $DB = 50, DF = 40,$   
 $NC = 40, EH = 30,$   
 $FE = 35, FG = 30,$   
 $OA = 20, KG = 20.$   
 $a_A, a_B, a_C - ?$

**Задача K9.6.**

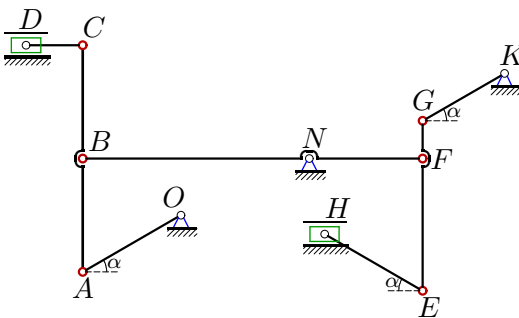
6



$\omega_{NB} = 1 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 20, BC = 10,$   
 $BF = 50, NF = 50,$   
 $CD = 25, EH = 30,$   
 $FG = 10, GE = 45,$   
 $OA = 20, KG = 25.$   
 $a_A, a_B, a_C - ?$

**Задача K9.7.**

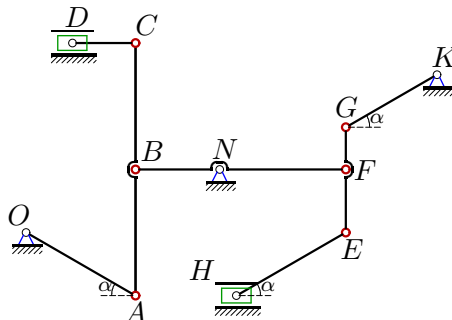
6



$\omega_{KG} = 1 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $NB = 60, NF = 30,$   
 $CD = 15, EH = 30,$   
 $FE = 35, FG = 10,$   
 $OA = 30, KG = 25.$   
 $a_G, a_F, a_E - ?$

**Задача K9.8.**

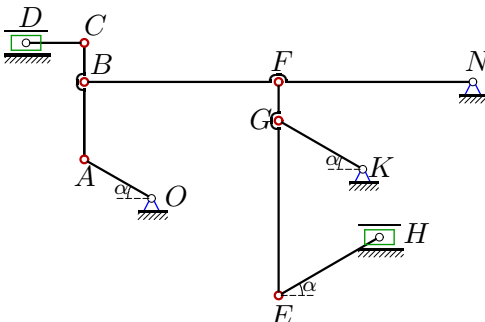
6



$\omega_{KG} = 1 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $NB = 20, NF = 30,$   
 $CD = 15, EH = 30,$   
 $FE = 15, FG = 10,$   
 $OA = 30, KG = 25.$   
 $a_G, a_F, a_E - ?$

**Задача K9.9.**

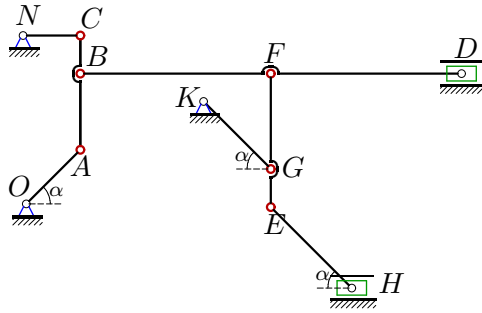
6



$\omega_{KG} = 2 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 20, BC = 10,$   
 $BF = 50, NF = 50,$   
 $CD = 15, EH = 30,$   
 $FG = 10, GE = 45,$   
 $OA = 20, KG = 25.$   
 $a_G, a_F, a_E - ?$

**Задача K9.10.**

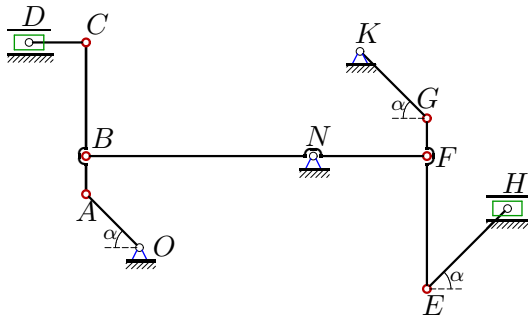
6



$\omega_{NC} = 1 \text{ рад/с}, \alpha = 45^\circ,$   
 $AB = 20, BC = 10,$   
 $BF = 50, FD = 50,$   
 $NC = 15, EH = 30,$   
 $FE = 35, FG = 25,$   
 $OA = 20, KG = 25.$   
 $a_A, a_B, a_C - ?$

**Задача K9.11.**

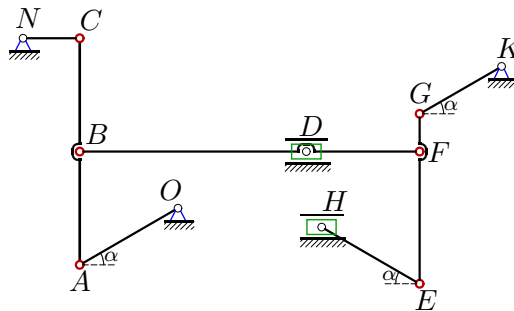
6



$\omega_{BF} = 1 \text{ рад/с}, \alpha = 45^\circ,$   
 $AB = 10, BC = 30,$   
 $NB = 60, NF = 30,$   
 $CD = 15, EH = 30,$   
 $FE = 35, FG = 10,$   
 $OA = 20, KG = 25.$   
 $a_A, a_B, a_C - ?$

**Задача K9.12.**

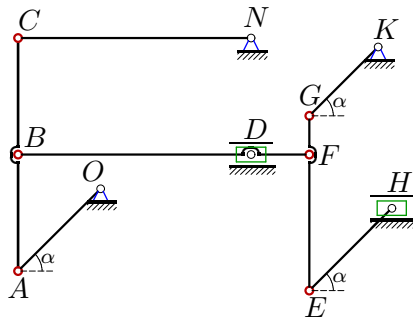
6



$\omega_{OA} = 2 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $DB = 60, DF = 30,$   
 $NC = 15, EH = 30,$   
 $FE = 35, FG = 10,$   
 $OA = 30, KG = 25.$   
 $a_A, a_B, a_C - ?$

**Задача K9.13.**

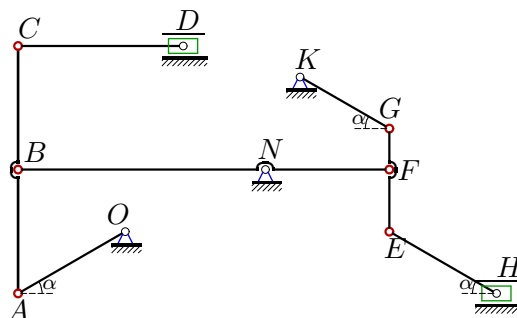
6



$\omega_{OA} = 1 \text{ рад/с}, \alpha = 45^\circ,$   
 $AB = 30, BC = 30,$   
 $DB = 60, DF = 15,$   
 $NC = 60, EH = 30,$   
 $FE = 35, FG = 10,$   
 $OA = 30, KG = 25.$   
 $a_A, a_B, a_C - ?$

**Задача K9.14.**

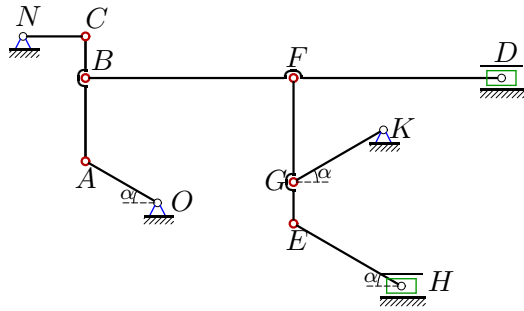
6



$\omega_{KG} = 2 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $NB = 60, NF = 30,$   
 $CD = 40, EH = 30,$   
 $FE = 15, FG = 10,$   
 $OA = 30, KG = 25.$   
 $a_G, a_F, a_E - ?$

Задача K9.15.

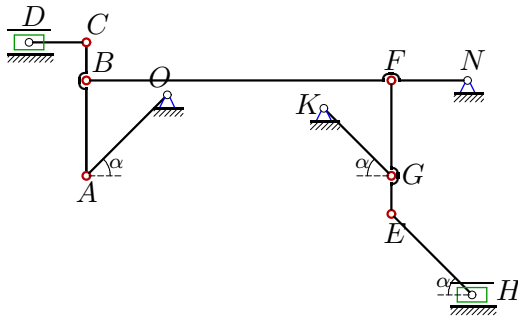
6



$\omega_{OA} = 2 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 20, BC = 10,$   
 $BF = 50, FD = 50,$   
 $NC = 15, EH = 30,$   
 $FE = 35, FG = 25,$   
 $OA = 20, KG = 25.$   
 $a_A, a_B, a_C - ?$

Задача K9.16.

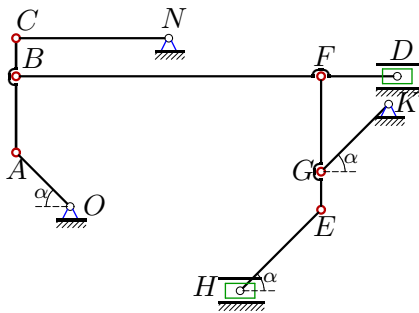
6



$\omega_{OA} = 1 \text{ рад/с}, \alpha = 45^\circ,$   
 $AB = 25, BC = 10,$   
 $BF = 80, NF = 20,$   
 $CD = 15, EH = 30,$   
 $FG = 25, GE = 10,$   
 $OA = 30, KG = 25.$   
 $a_A, a_B, a_C - ?$

Задача K9.17.

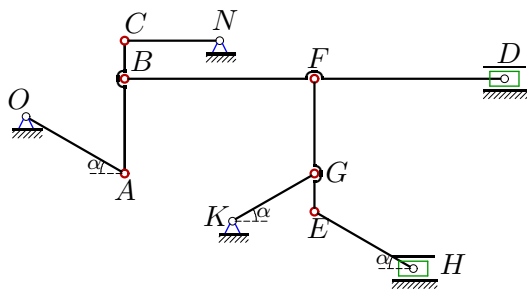
6



$\omega_{NC} = 1 \text{ рад/с}, \alpha = 45^\circ,$   
 $AB = 20, BC = 10,$   
 $BF = 80, FD = 20,$   
 $NC = 40, EH = 30,$   
 $FE = 35, FG = 25,$   
 $OA = 20, KG = 25.$   
 $a_A, a_B, a_C - ?$

Задача K9.18.

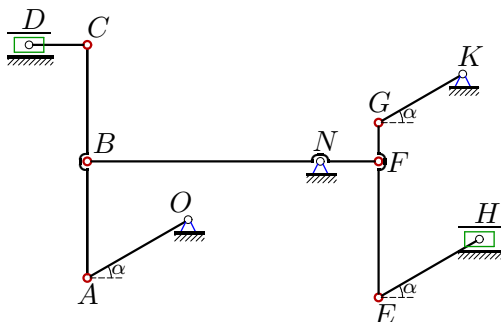
6



$\omega_{NC} = 1 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 25, BC = 10,$   
 $BF = 50, FD = 50,$   
 $NC = 25, EH = 30,$   
 $FE = 35, FG = 25,$   
 $OA = 30, KG = 25.$   
 $a_A, a_B, a_C - ?$

Задача K9.19.

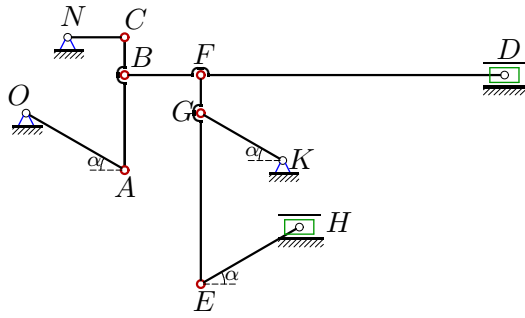
6



$\omega_{KG} = 3 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $NB = 60, NF = 15,$   
 $CD = 15, EH = 30,$   
 $FE = 35, FG = 10,$   
 $OA = 30, KG = 25.$   
 $a_G, a_F, a_E - ?$

Задача K9.20.

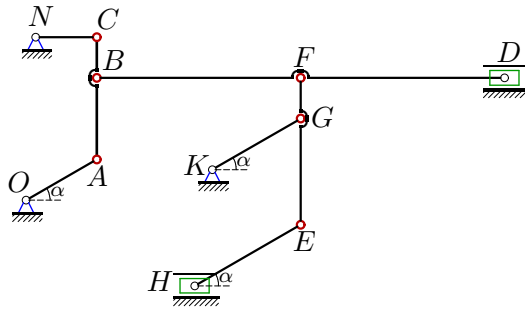
6



$\omega_{NC} = 3 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 25, BC = 10,$   
 $BF = 20, FD = 80,$   
 $NC = 15, EH = 30,$   
 $FE = 55, FG = 10,$   
 $OA = 30, KG = 25.$   
 $a_A, a_B, a_C - ?$

Задача K9.21.

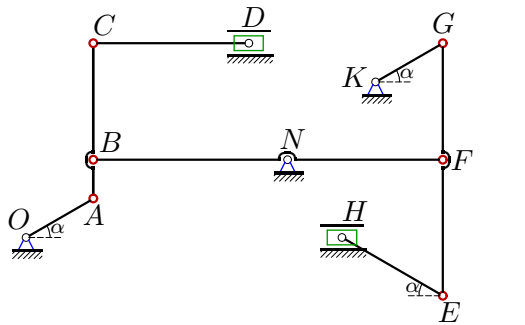
6



$\omega_{NC} = 1 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 20, BC = 10,$   
 $BF = 50, FD = 50,$   
 $NC = 15, EH = 30,$   
 $FE = 36, FG = 10,$   
 $OA = 20, KG = 25.$   
 $a_A, a_B, a_C - ?$

Задача K9.22.

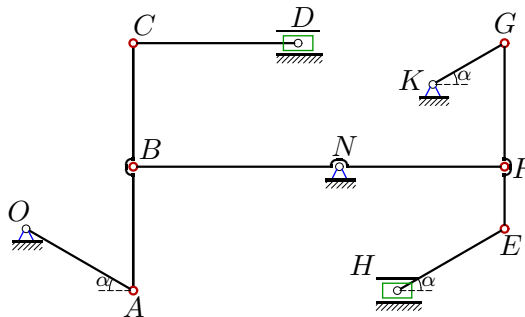
6



$\omega_{BF} = 1 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 10, BC = 30,$   
 $NB = 50, NF = 40,$   
 $CD = 40, EH = 30,$   
 $FE = 35, FG = 30,$   
 $OA = 20, KG = 20.$   
 $a_A, a_B, a_C - ?$

Задача K9.23.

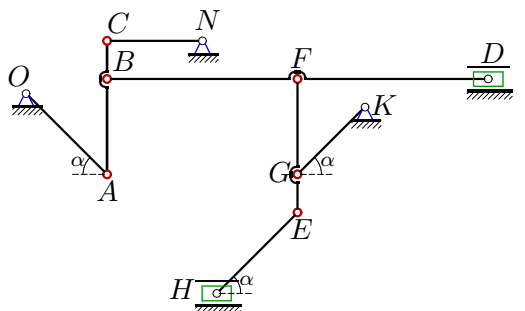
6



$\omega_{KG} = 3 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $NB = 50, NF = 40,$   
 $CD = 40, EH = 30,$   
 $FE = 15, FG = 30,$   
 $OA = 30, KG = 20.$   
 $a_G, a_F, a_E - ?$

Задача K9.24.

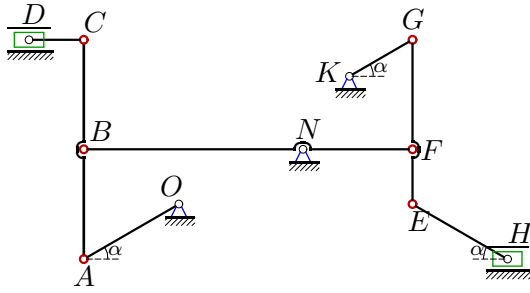
6



$\omega_{OA} = 1 \text{ рад/с}, \alpha = 45^\circ,$   
 $AB = 25, BC = 10,$   
 $BF = 50, FD = 50,$   
 $NC = 25, EH = 30,$   
 $FE = 35, FG = 25,$   
 $OA = 30, KG = 25.$   
 $a_A, a_B, a_C - ?$

Задача K9.25.

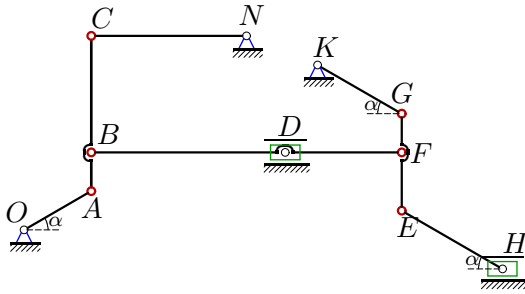
6



$\omega_{OA} = 2 \text{ рад/с}$ ,  $\alpha = 30^\circ$ ,  
 $AB = 30$ ,  $BC = 30$ ,  
 $NB = 60$ ,  $NF = 30$ ,  
 $CD = 15$ ,  $EH = 30$ ,  
 $FE = 15$ ,  $FG = 30$ ,  
 $OA = 30$ ,  $KG = 20$ .  
 $a_A$ ,  $a_B$ ,  $a_C$  - ?

Задача K9.26.

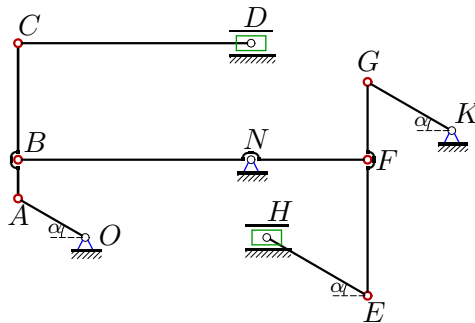
6



$\omega_{OA} = 4 \text{ рад/с}$ ,  $\alpha = 30^\circ$ ,  
 $AB = 10$ ,  $BC = 30$ ,  
 $DB = 50$ ,  $DF = 30$ ,  
 $NC = 40$ ,  $EH = 30$ ,  
 $FE = 15$ ,  $FG = 10$ ,  
 $OA = 20$ ,  $KG = 25$ .  
 $a_A$ ,  $a_B$ ,  $a_C$  - ?

Задача K9.27.

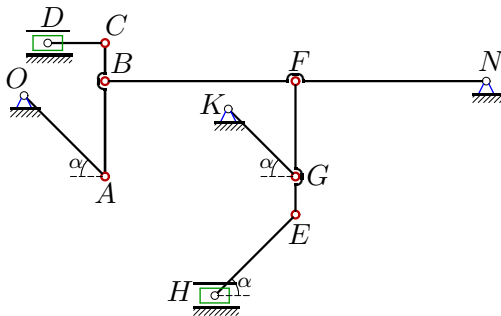
6



$\omega_{KG} = 4 \text{ рад/с}$ ,  $\alpha = 30^\circ$ ,  
 $AB = 10$ ,  $BC = 30$ ,  
 $NB = 60$ ,  $NF = 30$ ,  
 $CD = 60$ ,  $EH = 30$ ,  
 $FE = 35$ ,  $FG = 20$ ,  
 $OA = 20$ ,  $KG = 25$ .  
 $a_G$ ,  $a_F$ ,  $a_E$  - ?

Задача K9.28.

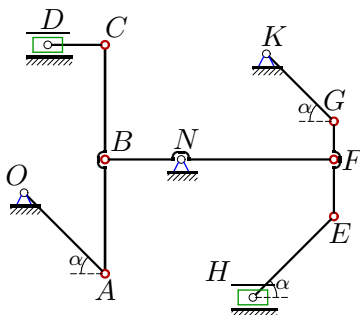
6



$\omega_{NB} = 1 \text{ рад/с}$ ,  $\alpha = 45^\circ$ ,  
 $AB = 25$ ,  $BC = 10$ ,  
 $BF = 50$ ,  $NF = 50$ ,  
 $CD = 15$ ,  $EH = 30$ ,  
 $FG = 25$ ,  $GE = 10$ ,  
 $OA = 30$ ,  $KG = 25$ .  
 $a_A$ ,  $a_B$ ,  $a_C$  - ?

Задача K9.29.

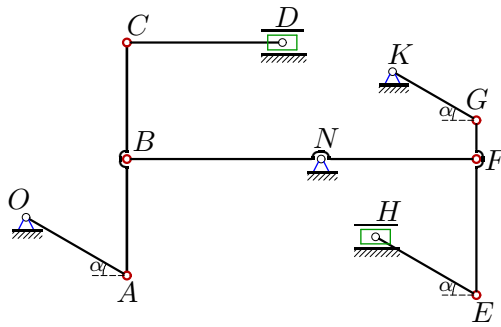
6



$\omega_{BF} = 3 \text{ рад/с}$ ,  $\alpha = 45^\circ$ ,  
 $AB = 30$ ,  $BC = 30$ ,  
 $NB = 20$ ,  $NF = 40$ ,  
 $CD = 15$ ,  $EH = 30$ ,  
 $FE = 15$ ,  $FG = 10$ ,  
 $OA = 30$ ,  $KG = 25$ .  
 $a_A$ ,  $a_B$ ,  $a_C$  - ?

Задача К9.30.

6



$\omega_{BF} = 2 \text{ рад/с}, \alpha = 30^\circ,$   
 $AB = 30, BC = 30,$   
 $NB = 50, NF = 40,$   
 $CD = 40, EH = 30,$   
 $FE = 35, FG = 10,$   
 $OA = 30, KG = 25.$   
 $a_A, a_B, a_C - ?$

**К9 Ответы.**  
**Кинематический анализ механизма (7 звеньев)**

04.04.2012

| №  | $v_A$   | $v_B$   | $v_C$   | $v_D$   | $v_E$   | $v_F$   | $v_G$   | $v_H$   |
|----|---------|---------|---------|---------|---------|---------|---------|---------|
| 1  | 60.000  | 52.915  | 51.962  | 10.000  | 36.056  | 27.839  | 30.000  | 10.000  |
| 2  | 90.000  | 77.942  | 90.000  | 45.000  | 62.650  | 51.962  | 60.000  | 5.000   |
| 3  | 80.000  | 69.282  | 72.111  | 20.000  | 44.542  | 34.641  | 40.000  | 48.000  |
| 4  | 30.000  | 25.981  | 30.000  | 15.000  | 14.156  | 12.990  | 15.000  | 1.875   |
| 5  | 184.752 | 174.356 | 160.000 | 69.282  | 268.766 | 145.547 | 147.802 | 162.428 |
| 6  | 115.470 | 100.000 | 104.083 | 28.868  | 166.458 | 50.000  | 57.735  | 187.639 |
| 7  | 50.000  | 43.301  | 50.000  | 25.000  | 48.814  | 21.651  | 25.000  | 31.250  |
| 8  | 16.667  | 14.434  | 16.667  | 8.333   | 28.641  | 21.651  | 25.000  | 31.250  |
| 9  | 100.000 | 86.603  | 90.139  | 25.000  | 144.157 | 43.301  | 50.000  | 162.500 |
| 10 | 21.213  | 15.811  | 15.000  | 5.000   | 14.577  | 9.014   | 10.607  | 5.000   |
| 11 | 84.853  | 60.000  | 189.737 | 180.000 | 109.202 | 30.000  | 42.426  | 75.000  |
| 12 | 60.000  | 54.083  | 51.962  | 15.000  | 122.780 | 30.000  | 30.000  | 105.000 |
| 13 | 30.000  | 23.717  | 21.213  | 10.607  | 66.503  | 11.859  | 7.500   | 71.595  |
| 14 | 100.000 | 86.603  | 100.000 | 50.000  | 57.282  | 43.301  | 50.000  | 62.500  |
| 15 | 40.000  | 35.277  | 34.641  | 6.667   | 24.037  | 18.559  | 20.000  | 26.667  |
| 16 | 30.000  | 21.213  | 22.847  | 8.485   | 7.299   | 4.243   | 6.000   | 1.697   |
| 17 | 56.569  | 42.164  | 40.000  | 13.333  | 18.367  | 15.549  | 11.314  | 8.533   |
| 18 | 28.868  | 25.338  | 25.000  | 4.124   | 17.158  | 13.163  | 14.434  | 18.970  |
| 19 | 300.000 | 259.808 | 300.000 | 150.000 | 146.442 | 64.952  | 75.000  | 168.750 |
| 20 | 51.962  | 45.608  | 45.000  | 7.423   | 88.559  | 36.757  | 41.569  | 101.696 |
| 21 | 17.321  | 15.275  | 15.000  | 2.887   | 11.026  | 8.036   | 8.660   | 3.753   |
| 22 | 57.735  | 50.000  | 100.000 | 86.603  | 48.228  | 40.000  | 46.188  | 3.849   |
| 23 | 75.000  | 64.952  | 75.000  | 37.500  | 54.083  | 51.962  | 60.000  | 45.000  |
| 24 | 30.000  | 22.062  | 21.213  | 6.061   | 20.270  | 12.216  | 15.000  | 6.667   |
| 25 | 60.000  | 51.962  | 60.000  | 30.000  | 27.042  | 25.981  | 30.000  | 7.500   |
| 26 | 80.000  | 75.498  | 69.282  | 30.000  | 57.000  | 51.264  | 48.000  | 15.000  |
| 27 | 200.000 | 173.205 | 346.410 | 300.000 | 123.111 | 86.603  | 100.000 | 137.500 |
| 28 | 141.421 | 100.000 | 107.703 | 40.000  | 86.023  | 50.000  | 70.711  | 120.000 |
| 29 | 84.853  | 60.000  | 84.853  | 60.000  | 216.333 | 120.000 | 169.706 | 60.000  |
| 30 | 115.470 | 100.000 | 115.470 | 57.735  | 180.370 | 80.000  | 92.376  | 207.846 |

| $N_0$ | $\omega_{OA}$ | $\omega_{CA}$ | $\omega_{CD}$ | $\omega_{BF}$ | $\omega_{FE}$ | $\omega_{KG}$ | $\omega_{EH}$ | $\omega_{NC}$ | $a_A$  | $a_B$  | $a_C$  | $a_E$  | $a_F$ | $a_G$ |
|-------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|--------|--------|--------|--------|-------|-------|
| 1     | 3.000         | -1.000        | -             | -0.520        | 1.000         | 1.200         | -1.000        | -2.078        | 1.800  | 1.118  | 1.614  | -      | -     | -     |
| 2     | 3.000         | 1.500         | 1.949         | 1.299         | 1.000         | 3.000         | 2.000         | -             | 2.700  | 1.217  | 0.313  | -      | -     | -     |
| 3     | 4.000         | -2.000        | -2.771        | -0.693        | 0.800         | 1.600         | -1.333        | -             | 3.200  | 2.448  | 3.503  | -      | -     | -     |
| 4     | 1.000         | 0.500         | 0.433         | 0.433         | -0.375        | -0.600        | 0.500         | -             | 0.300  | 0.135  | 0.035  | -      | -     | -     |
| 5     | -9.238        | 2.309         | -             | 3.200         | 4.773         | 7.390         | 4.927         | 4.000         | 21.047 | 14.194 | 6.400  | -      | -     | -     |
| 6     | -5.774        | 2.887         | 4.000         | 1.000         | 2.887         | -2.309        | -1.925        | -             | 8.819  | 1.000  | 5.889  | -      | -     | -     |
| 7     | -1.667        | -0.833        | 2.887         | -0.722        | -1.250        | 1.000         | -0.833        | -             | -      | -      | -      | 1.679  | 0.322 | 0.250 |
| 8     | 0.556         | 0.278         | 0.962         | -0.722        | -1.250        | 1.000         | -0.833        | -             | -      | -      | -      | 0.882  | 0.322 | 0.250 |
| 9     | 5.000         | -2.500        | -5.774        | 0.866         | -2.500        | 2.000         | 1.667         | -             | -      | -      | -      | 3.848  | 1.186 | 1.000 |
| 10    | 1.061         | -0.500        | -             | -0.150        | 0.500         | 0.424         | -0.354        | 1.000         | 0.400  | 0.232  | 0.150  | -      | -     | -     |
| 11    | 4.243         | -6.000        | -4.000        | 1.000         | -3.000        | 1.697         | -1.414        | -             | 9.407  | 0.600  | 26.021 | -      | -     | -     |
| 12    | 2.000         | 0.500         | -             | 0.866         | 3.000         | -1.200        | 1.000         | -3.464        | 1.200  | 0.648  | 1.855  | -      | -     | -     |
| 13    | 1.000         | 0.354         | -             | 0.354         | 1.591         | -0.300        | -0.250        | 0.354         | 0.300  | 0.226  | 0.156  | -      | -     | -     |
| 14    | 3.333         | 1.667         | 2.165         | 1.443         | -2.500        | 2.000         | -1.667        | -             | -      | -      | -      | 2.079  | 1.287 | 1.000 |
| 15    | 2.000         | -0.667        | -             | 0.346         | 0.667         | 0.800         | 0.667         | -2.309        | 0.800  | 0.575  | 0.961  | -      | -     | -     |
| 16    | 1.000         | 0.849         | -1.414        | 0.212         | -0.170        | -0.240        | 0.200         | -             | 0.300  | 0.055  | 0.045  | -      | -     | -     |
| 17    | 2.828         | -1.333        | -             | 0.400         | 0.853         | 0.453         | -0.377        | 1.000         | 2.846  | 1.212  | 0.400  | -      | -     | -     |
| 18    | -0.962        | -0.412        | -             | 0.250         | 0.454         | -0.577        | 0.481         | 1.000         | 0.293  | 0.098  | 0.250  | -      | -     | -     |
| 19    | -10.000       | -5.000        | 17.321        | -4.330        | -3.750        | 3.000         | 2.500         | -             | -      | -      | -      | 20.854 | 3.784 | 2.250 |
| 20    | 1.732         | 0.742         | -             | -0.450        | 1.336         | -1.663        | -1.386        | 3.000         | 0.948  | 1.231  | 1.350  | -      | -     | -     |
| 21    | 0.866         | -0.289        | -             | -0.150        | -0.144        | 0.346         | 0.289         | 1.000         | 0.189  | 0.163  | 0.150  | -      | -     | -     |
| 22    | -2.887        | 2.887         | 1.250         | 1.000         | 0.770         | 2.309         | 1.540         | -             | 2.546  | 0.500  | 9.550  | -      | -     | -     |
| 23    | -2.500        | -1.250        | 1.624         | 1.299         | 1.000         | 3.000         | 2.000         | -             | -      | -      | -      | 0.507  | 0.903 | 1.800 |
| 24    | 1.000         | 0.606         | -             | -0.212        | -0.667        | -0.600        | 0.500         | -0.849        | 0.300  | 0.138  | 0.198  | -      | -     | -     |
| 25    | 2.000         | 1.000         | -3.464        | 0.866         | 0.500         | 1.500         | -1.000        | -             | 1.200  | 0.541  | 0.139  | -      | -     | -     |
| 26    | 4.000         | -1.000        | -             | -1.386        | -0.600        | -1.920        | 1.600         | -1.732        | 3.200  | 2.460  | 2.332  | -      | -     | -     |
| 27    | -10.000       | 10.000        | -2.887        | -2.887        | 2.500         | 4.000         | -3.333        | -             | -      | -      | -      | 13.017 | 2.610 | 4.000 |
| 28    | -4.714        | -4.000        | -6.667        | 1.000         | -2.000        | -2.828        | -2.357        | -             | 6.743  | 1.000  | 3.913  | -      | -     | -     |
| 29    | -2.828        | -2.000        | -4.000        | 3.000         | -12.000       | 6.788         | 5.657         | -             | 2.501  | 1.800  | 5.917  | -      | -     | -     |
| 30    | -3.849        | -1.925        | 2.500         | 2.000         | -4.619        | 3.695         | 3.079         | -             | 4.626  | 2.000  | 8.563  | -      | -     | -     |